### Semester: III, IV Effective from June 2018

Semester	Paper	Name of the Paper	Hours	Credit	Marks
III	MTH-301	Advanced Calculus-I	3	3	70 (20 Internal + 50 External)
	MTH-302	Numerical Analysis – I	3	3	
	MTH-303	Differential Equations	3	3	
	EG	Mathematical Methods	2	2	
		Group of Symmetries – I			
IV	MTH-401	Advanced Calculus-II	3	3	
	MTH-402	Numerical Analysis – II	3	3	
	MTH-403	Introduction to Abstract Algebra	3	3	
	EG	Mathematical Modelling	2	2	
		Group of Symmetries – II			

### SEMESTER -III MTH-301

(Advanced Calculus-I)

### Effective from June 2018

Marks:70 (20 internal + 50 external) (3 Hours / Week - Credits : 3)

### Unit I:

Limits and Continuity of a function of two variables, Partial Differentiation, Total Differential, Composite function, Homogeneous functions, Euler'stheorem for Homogeneous functions.

### Unit II:

Taylor's theorem for functions of two variables, Maclaurian's expansions in power series, Jacobian.

### Unit III:

Vector point function, Differentiation of vector point function, Gradient, Divergence and Curl, their properties, Line Integral.

### Unit IV:

Surface Integral, Green's, Gauss' and Stoke's theorems (Only for Cartesian coordinates).

- 1. Shantinarayan, P. K. Mittal: A course of Mathematical Analysis, S.Chand and Co., New Delhi.
- 2. Hari Kishan : Differential Calculus, Atlantic Pub. & Distributors(P) Ltd., New Delhi.
- 3. T. M. Apostol: Mathematical Analysis, Narosa Publishing House, New Delhi.
- 4. S. C. Malik: Mathematical Analysis, Wiley-Eastern Ltd, New Delhi.
- 5. N. P. Bhamore & et el: Mathematics Paper III–IV, Popular Prakashan, Surat.

### SEMESTER -III MTH-302

(Numerical Analysis–I)\*

### **Effective from June 2018**

Marks:70 (20 internal + 50 external) (3 Hours / Week - Credits : 3)

### Unit I:

Error estimation: Errors and their computations, A general error formula.

### Unit II:

Numerical Solutions of Algebraic and Transcendental Equations: Bisection Method, Method of False position, Iteration Method, Newton-Raphson's Method.

### Unit III:

Forward Differences, Backward Differences, Central Differences, Symbolic relation and separation of symbols, Differences of Polynomials.

### Unit IV:

Newton's Forward and Backward Formulae, Gauss' Interpolation formulae.

- 1. S. S. Sastry: Introductory methods of Numerical Analysis, Prentice-Hall of India Pvt. Ltd.; 4<sup>th</sup> Edition.
- 2. M. K. Jain, Iyenger, Jain: Numerical Methods for Scientific and Engineering Computations, New Age International Ltd.
- 3. Goel, Mittal: Numerical Analysis, Pragati Prakashan, Meerut.
- 4. Kaiser A. Kunz: Numerical Analysis, Mc Graw Hill Book Co., London.
- 5. James I. Buchanan, Peter R. Turner: Numerical Methods and Analysis, Mc Graw Hill Book Co., London.
- 6.P.C.Biswal:NumericalAnalysis,Prentice-HallofIndia, 2008.
- 7.H.C.Saxena: Finite Differences and Numerical Analysis, S. Chandand Co., 2005.

\* Use of Scientific non – programmable calculator is allowed.

# VEER NARMAD SOUTH GUJARAT UNIVERSITY, SURAT. SYLLABUS FOR B.Sc.(MATHEMATICS) SEMESTER -III

### MTH-303

(Differential Equations)

### Effective from June 2018

Marks:70 (20 internal + 50 external) (3 Hours / Week - Credits : 3)

### Unit I:

Linear Differential Equations with variable coefficients, Homogeneous Differential Equations, Legendre's Differential Equation.

### Unit II:

Second order Differential Equations: Solution in terms of known Integral, Solution by method of removal of first order derivatives, Method of Changing Independent Variable.

#### Unit III:

Formation of Partial Differential Equation, Solution of Partial Differential Equations, Equations solvable by direct integral.

### Unit IV:

Partial Differential Equations of first order, Nonlinear Partial Differential Equations of first order, Some special methods.

- 1. D. A. Murray: An Introductory Course in Differential Equations, Orient Longmans, Bombay.
- 2. I. N. Sneddon: Elements of Partial Differential Equations, McGraw HillBook Company.
- 3. B. S. Grewal: Higher Engineering Mathematics, Khanna Publishers, NewDelhi.
- 4. Gorakhprasad : Differential Equations, Pothishala Pvt. Ltd., Allahabad.
- 5. M. D. Rai Singhania: Differential Equations, S. Chand & Co., New Delhi.

- 6. Nita H. Shah: Ordinary and Partial Differential Equations: Theory and Applications, PHI Learning Pvt. Ltd, New Delhi.
- 7. N. P. Bhamore & et el. : Mathematics Paper III–IV, Popular Prakashan, Surat.

**SEMESTER-III** 

Elective Generic (Mathematical Methods)\*

**Effective from June 2018** 

Marks:70 (20 internal + 50 external) (2 Hours / Week - Credits : 2)

### Unit I:

Notations of finite difference calculus, Operators E, ,  $\nabla$ , $\delta$  relations between different operators and their prosperities, relation between difference and differential operators, Method of constructing difference tables, Finding the missing terms.

### Unit II:

Factorial notation, expression of polynomials in factorial notation by using finite differences, Method of unknown coefficients.

#### Unit III:

Difference equations: Order and degree of a difference equation, Solution of difference equations, homogeneous difference equations with constant coefficients.

- 1. S.S. Sastry: Introductory methods of Numerical Analysis, Prentice-Hall of India Pvt. Ltd.; 4<sup>th</sup> Edition.
- 2. M. K. Jain, Iyenger, Jain: Numerical Methods for Scientific and Engineering Computations, New Age International Ltd.
- 3. Goel, Mittal: Numerical Analysis, Pragati Prakashan, Meerut.
- 4. Kaiser A. Kunz: Numerical Analysis, McGraw Hill Book Co., London.
- 5. James I. Buchanan, Peter R. Turner: Numerical Methods & Analysis, McGraw Hill Book Co., London.

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### VEER NARMAD SOUTH GUJARAT UNIVERSITY, SURAT. SYLLABUS FOR B.Sc. (MATHEMATICS)

**SEMESTER - III** 

Elective Generic (Group of Symmetries-I)

Effective from June 2018

Marks:70 (20 internal + 50 external) (2 Hours / Week - Credits : 2)

### Unit I:

Definition of a group, its elementary properties, order of a group, order of an element of a group, Group multiplication tables, Examples of groups including finite groups, infinite groups, Abelian groups, Cyclic groups.

### Unit II:

Subgroup, condition that a subset is a subgroup, Examples of subgroups, Basic concept of symmetry, Symmetry elements and symmetry operations in a space, Identity symmetry operation.

### Unit III:

Symmetry planes and reflection symmetry, Inversion centre and inversion symmetry, Rotation axes and rotation symmetry, Improper axes and improper rotation symmetry, product of symmetry operations.

- 1. F.A. Cotton: Chemical application of group theory, Wiley Inter Science, Wiley Eastern Ltd., New Delhi.
- 2. G.Davidson: Intro. Group Theory for Chemists, Applied Science Publisher.
- 3. I.N.Herstein: Topics in Algebra, Wiley Eastern Ltd., New Delhi.

### SEMESTER -IV MTH-401

(Advanced Calculus-II)

### Effective from June 2018

Marks:70 (20 internal + 50 external) (3 Hours / Week - Credits : 3)

### Unit I:

Maxima-Minima for functions of two variables: Necessary and sufficient conditions for extreme points.

### Unit II:

Double and Triple Integrals: Change of order of Double integrals, Area.

### Unit III:

Beta-Gamma functions: Relation between Beta and Gamma functions, Properties, Applications of Beta-Gamma function.

### Unit IV:

Laplace Transforms: Laplace Transform of elementary functions, Properties of Laplace Transform, Differentiation and Integration of Laplace Transform, Laplace Transform of derivatives and integrals.

Inverse of Laplace Transform: Method of Partial fractions, Properties of inverse Laplace Transform.

### The course is covered by the following reference books:

- 1. David V. Widder: Advanced Calculus, PHI Learning Pvt. Ltd, New Delhi
- 2. Kreysig: Advanced Engineering Mathematics, John Wiley, New York, 1999.
- 3. Shantinarayan, P. K. Mittal: A course of Mathematical Analysis, S. Chand and

Co., New Delhi.

4. N. P. Bhamore & et al: Mathematics Paper III-IV, Popular Prakashan, Surat.

### SEMESTER -IV MTH-402

(Numerical Analysis-II)\*

### Effective from June 2018

Marks:70 (20 internal + 50 external) (3 Hours / Week - Credits : 3)

### Unit I:

Finite difference with unequal interval, Lagrange's Interpolation Formula, Divided Differences, Newton's General Interpolation Formula.

### Unit II:

Numerical Differentiation: 1<sup>st</sup> and 2<sup>nd</sup> order derivatives based on Newton's forward andbackward difference interpolation formulae.

### Unit III:

Numerical Integration: General Integration formula, Trapezoidal Rule, Simpson's 1/3-Rule, Simpson's 3/8-Rule.

### Unit IV:

Solution of Ordinary Differential Equations by Taylor's series method, Picard's approximation method, Euler's method.

- 1. S.S. Sastry: Introductory methods of Numerical Analysis, Prentice-Hall of India Pvt. Ltd.; 4<sup>th</sup> Edition.
- 2. M. K. Jain, Iyenger, Jain: Numerical Methods for Scientific and Engineering Computations, New Age International Ltd.
- 3. Goel, Mittal: Numerical Analysis, Pragati Prakashan, Meerut.
- 4. Kaiser A. Kunz: Numerical Analysis, McGraw Hill Book Co., London.
- 5. James I. Buchanan, Peter R. Turner: Numerical Methods and Analysis, McGraw Hill Book Co., London.

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### VEER NARMAD SOUTH GUJARAT UNIVERSITY, SURAT. SYLLABUS FOR B.Sc.(MATHEMATICS) SEMESTER -IV

MTH-403

(Introduction to Abstract Algebra)

Effective from June 2018

Marks:70 (20 internal + 50 external) (3 Hours / Week - Credits : 3)

#### Unit I:

Divisors, Greatest common divisor, Least Common multiple, Prime numbers, Fundamental theorem of Arithmetic, Congruence relation, Equivalence classes.

#### Unit II:

Definition of a Group, Examples of Group, elementary properties of a Group, Finite Groups.

### Unit III:

Subgroups, Cyclic Groups, Order of an element.

### Unit IV:

Definition of a Ring, Examples of Ring, Integral Domain, Field, Boolean Ring.

- 1. I. N. Herstein: Topics in Algebra, Wiley Eastern Ltd., New Delhi, 2006.
- 2 I. H. Sheth: Abstract Algebra, Nirav Prakashan, Ahmedabad.
- 3. N. S. Gopal Krishnan: University Algebra, Wiley Eastern Ltd.
- 4. P. R. Bhattacharya, S. K. Jain and S. R. Nagpaul: Basic Abstract Algebra, Cambridge University Press, Indian Edition, 1997.
- 5. Shantinarayan: Modern Algebra, S. Chand and Co., New Delhi.
- 6. Serge Lang: Algebra, Addition Wesley, 1993.
- 7. Surjeet, Kazi Zameeruddin: Modern Algebra, Vikas Publishing House.

**SEMESTER -IV** 

Elective Generic (Mathematical Modelling)\*

**Effective from June 2018** 

Marks:70 (20 internal + 50 external) (2 Hours / Week - Credits : 2)

### Unit I:

Mathematical modelling through ordinary differential equation of first order, Linear growth models; Linear decay models, Models for growth of Science and scientists.

### Unit II:

Non-linear growth and decay models, Model of Logistic law of population, Spread of technological innovation, Spread of infectious diseases.

#### Unit III:

Mathematical models of geometrical problems through ordinary differential equation of first order, Simple geometrical problems, Orthogonal trajectories.

- 1. J. N. Kapoor: Mathematical Modelling, New Age International Publishers, New Delhi.
- 2. Kreysig: Advanced Engineering Mathematics, John Wiley, New York, 1999.
- 3. J. K. Sharma: OR Theory & Applications, Mac Milian India Ltd., 1998.
- 4. G. Hadley: Linear Programming, Narosa Publishing House, New Delhi,1995.
- 5. G. Paria: Linear Programming, Transportation, Assignment, Game, Books & Allied Pvt. Ltd. Calcutta.

<sup>\*</sup> Use of Scientific non – programmable calculator is allowed.

**SEMESTER - IV** 

**Elective Generic** (Group of Symmetries-II)

**Effective from June 2018** 

Marks:70 (20 internal + 50 external) (2 Hours / Week - Credits : 2)

### Unit I:

Formation of groups of symmetries (in space) of the following Plane figures (regarded as rigid objects):

- 1. An isosceles triangle (cyclic group C<sub>2</sub> of order 2)
- 2. An equilateral triangle (the group  $S_3$  of order 6)
- 3. A rectangle (the group  $V_4$ )
- 4. A square (the group  $D_4$ )

#### Unit II:

Formation of groups of symmetries of the following Chemical Molecules (Configuration of atoms).

- 1.  $H_2O$  (the group  $V_4$ )
- 2.  $H_2O_2$
- 3. Trans-  $N_2 F_2$  (the group  $V_4$ )
- 4.  $NH_3$ ,  $PCl_3$ ,  $CHCl_3$ (the group  $S_3$ )

#### Unit III:

Concept of isomorphism of groups, Isomorphism of multiplicative group with the group  $C_2$  of the symmetries of an isosceles triangle, Isomorphism of multiplicative group with the group  $V_4$  of the symmetries of a rectangle, Isomorphism of group  $V_4$  of the symmetries of a rectangle with the group of symmetries of  $H_2O$ , Isomorphism of group  $S_3$  of the symmetries of an equilateral triangle with the group of symmetries of  $NH_3$ ,  $PCl_3$ ,  $CHCl_3$ .

- 1. F.A. Cotton: Chemical application of group theory, Wiley Inter Science Wiley Eastern Ltd., New Delhi.
- G. Davidson: Intro. Group Theory for Chemists, Applied Science Publisher.
   I. N. Herstein: Topics in Algebra, Wiley Eastern Ltd., New Delhi, 2006.